(a)


(b)

(c)




(e)



Procedures for performing the polarization measurement. (a-d) are the UQSD measurement strategy, (e) is the MED measurement strategy. (a) In UQSD, when $\tan 2 \theta_{\mathrm{a}}>\sin 2 \theta_{\mathrm{n}}$, the H 4 rotates the polarization by $2 \theta_{4}$, thereby transforming $\left|d_{2}\right\rangle$ to $|h\rangle$. (b) Then the horizontal component is divided into two parts by H 5 , one part is the common state $\left(\left|d_{2}\right\rangle\right)$, and the other is transformed to $|v\rangle$ by H6, which is set at $45^{\circ}$. (c) The residual $\left(\left|q_{1}\right\rangle\right.$ and $\left.\left|q_{3}\right\rangle\right)$ is unambiguously discriminated by H 7 followed by a PBS. (d) When $\tan 2 \theta_{\mathrm{a}}<\sin 2 \theta_{\mathrm{n}}$, the H4 rotates $\left|d_{2}\right\rangle$ to $|h\rangle$. Then the states are projected to the basis states $|h\rangle$ and $|v\rangle$. When we detect the photon in the $|v\rangle$ state, we assert that the photon is in the state $\left|d_{1}\right\rangle$. Otherwise, we obtain an inconclusive result. (e) In MED, the H 4 rotates the polarization suitably to minimize the guessing error.

