Quantum Squeezing Induced Optical Nonreciprocity

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We propose an all-optical approach to achieve optical nonreciprocity on a chip by quantum squeezing one of two coupled resonator modes. By parametric pumping a $\chi^{(2)}$-nonlinear resonator unidirectionally with a classical coherent field, we squeeze the resonator mode in a selective direction due to the phase-matching condition, and induce a chiral photon interaction between two resonators. Based on this chiral interresonator coupling, we achieve an all-optical diode and a three-port quasicirculator. By applying a second squeezed-vacuum field to the squeezed resonator mode, our nonreciprocal device also works for single-photon pulses. We obtain an isolation ratio of > 40 dB for the diode and fidelity of > 98% for the quasicirculator, and insertion loss of < 1 dB for both. We also show that nonreciprocal transmission of strong light can be switched on and off by a relative weak pump light. This achievement implies a nonreciprocal optical transistor. Our protocol opens up a new route to achieve integrable all-optical nonreciprocal devices permitting chip-compatible optical isolation and nonreciprocal quantum information processing.

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Optical nonreciprocal devices, such as optical diodes and circulators, can separate backscattering signals from a light source. The conventional magneto-optical approach to achieve optical nonreciprocity (ONR) is difficult to integrate on a chip because it requires strong magnetic fields and bulky materials [1,2]. Developing a new mechanism for magnetic-free ONR is of interest in fundamental physics and promises important applications for on-chip light manipulation. Various magnetic-free optical nonreciprocal devices have been theoretically proposed and experimentally demonstrated by exploiting optical nonlinearities [3–11], spatiotemporal modulation of the medium [12–14], spin-momentum locking in chiral quantum optical systems [15–23], directional optomechanical coupling [24–26], moving atomic lattices [27–29], atomic reservoir engineering [30], the Sagnac effect in spinning resonators [31–33], and susceptibility-momentum locking in atomic gases [34–40]. Kerr-nonlinear optical nonreciprocal devices are compatible with a chip, but subject to dynamic reciprocity [6]. Despite many efforts, it is challenging to realize a chip-compatible all-optical nonreciprocal device without moving parts or spatiotemporal modulation. By directionally amplifying the single-photon interaction in a $\chi^{(2)}$ microring resonator via the mode mean field, one can induce chiral normal mode splitting (NMS) and construct on-chip optical isolators [41]. Nevertheless, the demanded three-mode phase matching in one resonator is a significant challenge [42], and normally leads to an inefficient detuned driving, resulting in a weak ONR and a large insertion loss [41].

Quantum squeezing of a $\chi^{(2)}$ resonator mode can exponentially amplify the interaction between quantum objects. It could solve various challenging tasks [43–52]. Nevertheless, it is still an open question how to achieve ONR via quantum squeezing. Here, we show that high-performance ONR can be achieved by directionally squeezing the resonator mode with a coherent laser field. With this chiral quantum squeezing, we achieve an optical diode, a quasicirculator and, for the first time, a nonreciprocal optical transistor. Note that our method is based on directional quantum squeezing and thus conceptually differs from Ref. [41]. Our method only needs two-mode matching in one resonator and thus greatly simplifies its experimental implementation.

The schematic of our proposed system is depicted in Fig. 1. It consists of two coupled whispering-gallery mode microring resonators and two nearby optical waveguides. The resonators can be made of high-quality thin film with $\chi^{(2)}$ nonlinearity, e.g., lithium niobate or aluminum nitride. Thus, the resonators support the parametric nonlinear optical process. The resonator $B (R_B)$ is pumped from port 3 by a continuous wave coherent laser field with frequency $\omega_p$, amplitude $|a_p|$, and phase $\theta_p$. This classical pump generates a squeezing interaction with strength $\Omega_p$, for the counterclockwise (CCW) mode $b_{\uparrow\downarrow}$. Because of the
FIG. 1. Schematic of an all-optical nonreciprocal system consisting of two microring resonators ($R_A$ and $R_B$) and two nearby optical waveguides (WG1 and WG2). To achieve classical light isolation, a coherent pump field is applied to generate a CCW squeezing mode $b_{\circledast}$ in $R_B$. To achieve single-photon isolation, a broadband squeezed-vacuum field is used to drive $R_B$. (a) A forward-input signal field excites a CW mode $a_{\circledast}$ in $R_A$, which interacts with the squeezed mode $b_{\circledast}$ with a coupling rate $J_s$. (b) A backward-input signal field stimulates a CCW mode $a_{\circledast}$ in $R_A$. It couples to a CW bare mode $b_0$ in $R_B$ with a bare coupling rate $J_0$.

directional phase-matching condition in the parametric nonlinear process, the mode $b_{\circledast}$ is squeezed to a mode $b_{\circledast}$, but the clockwise (CW) mode $b_{\circledast}$ is unsqueezed. The resonator $A$ ($R_A$) slightly differs in size from $R_B$, such that the pump field cannot drive the parametric nonlinear process in the former. In this arrangement, we only need to consider mode squeezing in $R_B$.

Now we discuss how the pump laser modulates the inter-resonator interaction and causes the ONR. In the forward-input case, a signal field input to port 1 excites the CW mode $a_{\circledast}$ in $R_A$. Because of the pump field, the mode $a_{\circledast}$ couples to the squeezed mode $b_{\circledast}$ with a rate $J_s$. The pump also causes a frequency shift to $b_{\circledast}$ with respect to the bare mode $b_0$. In comparison, in the backward-input case, a signal field from port 2 excites the CCW mode $a_{\circledast}$ in $R_A$. In this case, the pump field has no action on the CW mode $b_{\circledast}$. This case is equivalent to the unpumped system only consisting of two resonators. Thus, the mode $a_{\circledast}$ interacts with the bare mode $b_0$ with an unmodulated coupling rate $J_0$.

In the frame rotating at frequency $\omega_p / 2$, the Hamiltonian for the forward-input case reads

$$\mathcal{H}_\text{fw} = \mathcal{H}_A + \mathcal{H}_B + \mathcal{H}_J,$$

$$\mathcal{H}_A / h = \Delta^b_{a} a^\dagger_{\circledast} a_{\circledast} + i \sqrt{\Delta^b_{a} a^\dagger_{\circledast} a_{\circledast} - a^\dagger_{\circledast} a_{\circledast} e^{i\Delta_m}},$$

$$\mathcal{H}_B / h = \Delta^b_{b} b^\dagger_{\circledast} b_{\circledast} + \Omega_p (e^{-i\theta} b^\dagger_{\circledast} b_{\circledast} + e^{i\theta} b^\dagger_{\circledast} b_{\circledast}),$$

$$\mathcal{H}_J / h = J_0 (a^\dagger_{\circledast} a_{\circledast} + a_{\circledast} b^\dagger_{\circledast}),$$

where the detunings are $\Delta^b_{a/b} = \omega_{a/b} - \omega_p / 2$ and $\Delta_m = \omega_m - \omega_p / 2$, $\omega_{a/b}$ is the resonance frequency of $R_{A/B}$, $\omega_m$ is the frequency of the signal mode $a_{m}$, and $\kappa_{ex}$ is the external decay rate of $R_A$. The pump strength $\Omega_p$ is created by driving a mode $e_{\circledast}$ of $R_B$ with an external field $a_{p}$. It is determined by the pump laser power $P_p$ (see Supplemental Material [53] for the detailed derivation and relation of $\Omega_p$ and $P_p$).

Applying the Bogoliubov squeezing transformation $[43,44,56,57]$ $b_\circledast = \cosh(r_p) b + e^{-i\theta b} \sinh(r_p) b^\dagger$ with the squeezing parameter $r_p = \frac{1}{2} \text{ln}(1 + \beta)/(1 - \beta)$ and $\beta = \Omega_p / \Delta^b_{p}$. We can transform the Hamiltonian $\mathcal{H}_\text{fw}$ to the squeezing picture. We further apply the rotating-wave approximation $\Delta^b_{p} + \Delta^b_{p} \sqrt{1 - \beta^2} \gg \sinh(r_p) J_0$ in the squeezing picture and neglect the counterrotating terms. Then, the Hamiltonian in the frame rotating at frequency of $\Delta_m$ becomes

$$\mathcal{H}_\text{fw} / h = \Delta_a a^\dagger_{\circledast} a_{\circledast} + i \sqrt{2 \Delta^b_{a} a^\dagger_{\circledast} a_{\circledast} - a^\dagger_{\circledast} a_{\circledast} e^{i\Delta_m}} + \Delta^b_{b} b^\dagger_{\circledast} b_{\circledast} + J_s (a^\dagger_{\circledast} b_{\circledast} + b^\dagger_{\circledast} a_{\circledast}),$$

where $\Delta_a = \omega_a - \omega_m$, $\Delta^b_{a} = \Delta^b_{p} - \Delta_m$, $\Delta^b_{b} = \Delta^b_{p} \sqrt{1 - \beta^2}$ and $J_s = \cosh(r_p) J_0$.

The effective squeezing mode detuning $\Delta^b_{a}$ and the effective coupling rate $J_s$ are controlled by the pump field $\Omega_p$ and the corresponding detuning $\Delta^b_{b}$. When the ratio $\beta$ approaches unity, the rate $J_s$ between $a_{\circledast}$ and $b_{\circledast}$ is enhanced exponentially with respect to the rate $J_0$ [53].

In the squeezing picture, the master equation of the system without a squeezed-vacuum driving takes the form $d\rho_{fw} / dt = -i [\mathcal{H}_\text{fw}, \rho_{fw}] + \mathcal{L}[\rho_{fw}]$, where $\mathcal{L}[\rho_{fw}]$ is the system density matrix, the term $\mathcal{L}_{\rho_{fw}}$ describes the decay of the mode $a_{\circledast}$ ($b_{\circledast}$) with a rate $\kappa_a$ ($\kappa_b$), and $\mathcal{L}[\rho] = 2 \rho o^\dagger o + o^\dagger \rho o - \rho o^\dagger o$. Here, $\kappa_a = \kappa_{ex} + \kappa_i$, where $\kappa_i$ is the intrinsic decay rate of $R_A$. The term $\mathcal{L}_{\rho_{fw}}$ describes the effective thermalization noise of the mode $b_{\circledast}$ resulting from the classical coherent pump. It is given by $\mathcal{L}_{\rho_{fw}} = N_p \mathcal{L}_{\rho_{fw}} + N_p \mathcal{L}_p L^\dagger_{\rho_{fw}} - M_p \mathcal{L}_p L^\dagger_{\rho_{fw}} - M_p \mathcal{L}_p L^\dagger_{\rho_{fw}}$, where $N_p = \sinh^2(r_p)$, $M_p = e^{i\theta b} \cosh(r_p) \sinh(r_p)$, and $\mathcal{L}[\rho] = 2 \rho o^\dagger o - \rho o - \rho o^\dagger o$. This noise can limit the application of the system in the quantum regime.

For achieving single-photon isolation, we can apply a broadband squeezed-vacuum field to cancel the pump-induced noise associated term $\mathcal{L}_{\rho_{fw}}$ [43,44,48,53]. Such broadband squeezed-vacuum field has been realized via optical parametric amplification [58]. In doing so, the mode $a_{\circledast}$ can couple to the squeezed mode $b_{\circledast}$ coherently without additional noise, just as a simple linear resonator system. The squeezed mode is equivalently coupled to a normal vacuum bath and has a decay rate of $\kappa_b$.

For the backward-input case, the Hamiltonian reads $\mathcal{H}_\text{bw} / h = \Delta_a a^\dagger_{\circledast} a_{\circledast} + i \sqrt{2 \Delta^b_{a} a^\dagger_{\circledast} a_{\circledast} - a^\dagger_{\circledast} a_{\circledast} e^{i\Delta_m}} + \Delta^b_{b} b^\dagger_{\circledast} b_{\circledast} + J_0 (a^\dagger_{\circledast} b_{\circledast} + b^\dagger_{\circledast} a_{\circledast})$, where $\Delta^b_{b} = \omega_b - \omega_m$. Comparing the Hamiltonians $\mathcal{H}_\text{fw}$ and $\mathcal{H}_\text{bw}$, we can see that the intermediate detuning and coupling in these two Hamiltonians can be very different due to the directional quantum squeezing. The dynamics of the system is governed by the master
We have used transmission from port \( \Lambda \) for the forward-input (backward-input) case \([53]\). By \( p \) replacing \( T \), and \( d \) in, we have \( \langle a_{\text{in}} \rangle \) for the steady-state solutions and \( \langle b_{\text{in}} \rangle \), and the steady-state transmissions.

We can also analytically derive the transmissions from the Langevin equations of motion. To consider the pump-induced noise, we truncate the Langevin equations to second-order nonlinear terms of operators and obtain

\[
\begin{align*}
\dot{a}_i &= -i(\Delta_a + \kappa_a) a_i + \sqrt{2\kappa_{\text{ext}}} a_i - iJ_a b_i, \\
\dot{b}_i &= -i(\Delta_b + \kappa_b) b_i - iJ_a a_i, \\
\dot{a}_j &= (i\Delta_{ab} - \kappa_{\text{ab}}) a_j + \sqrt{2\kappa_{\text{ext}}} a_j b_j - iJ_b \Xi, \\
\dot{b}_j &= iJ_b (a_j b_j - a_j b_j^\dagger) - iJ_a a_j b_j + \Psi_{\text{noise}}, \\
\dot{a}_i a_j &= -2\kappa_a a_i^\dagger a_j - (iJ_e a_i^\dagger b_j - \sqrt{2\kappa_{\text{ext}}} a_i a_j + \text{H.c.}),
\end{align*}
\]

where the pump-induced noise \( \Psi_{\text{noise}} = 2 \sinh^2 (r_p) \kappa_b \) is present in the forward-input case and plays the role of a thermal bath. In the backward-input case, \( \Psi_{\text{noise}} \) is absent. We have used \( \Delta_{ab} = \Delta_a - \Delta_b, \ k_{\text{ab}} = \kappa_a + \kappa_b \), and \( \Xi = a_i^\dagger a_j - a_i a_j^\dagger \). In the calculations, we need to, respectively, replace \( a, b, J, \Delta_a \) with \( a_{\text{opt}}, b_{\text{opt}}, J_{\text{opt}} \), \( a_{\text{opt}}, b_{\text{opt}}, J_{\text{opt}} \), and \( \Delta_{ab} \) for the forward-input (backward-input) case [53]. By solving the Langevin equations and using the input-output relations, we obtain the steady-state transmissions

\[
\begin{align*}
T_{12} &= (J_1^4 - 2\zeta_x J_1^2 + \Lambda_1)/G_s + 2\kappa_{\text{ext}} N_{\text{noise}}/|\alpha_{\text{in}}|^2, \\
T_{21} &= (J_0^4 - 2\zeta_x J_0^2 + \Lambda_0)/G_0, \quad T_{23} = 4\kappa_{\text{ext}} J_0^2 G_0/G_0.
\end{align*}
\]

where \( N_{\text{noise}} = \kappa_b(\kappa_a + \kappa_b) \sinh^2 (r_p) J_0^2/\mathcal{Q} \) is the number of noise-related photons, \( \mathcal{Q} = J_1^2(\kappa_a + \kappa_b)^2 + \kappa_b \kappa_b ([\kappa_a + \kappa_b]^2 + \Delta_{ab}^2), \ G_s = J_1^2 + 2J_1^2(\kappa_a b_b - \Delta_{ab} \Delta_b), \ G_b = J_0^2 + 2J_0^2(\kappa_a b_b - \Delta_{ab} \Delta_b), \ \zeta_x = \kappa_a b_b - 2\kappa_b \kappa_{\text{ext}} - \Delta_{\text{ext}} \Delta_b, \) and \( \Lambda_1 = (\kappa_a - 2\kappa_{\text{ext}})^2 + \Delta_{\text{ext}}^2(\kappa_a^2 + \Delta_{\text{ext}}^2) \) with \( x = \{s, 0\} \).

We define the isolation ratio as \( \eta = 10 \log_{10} (T_{12}/T_{21}) \).

By applying the squeezed-vacuum field to cancel the noise \( \Psi_{\text{noise}} \), the steady-state noise-free transmissions become

\[
T_{12}^\text{sv} = (J_1^4 + 2\zeta_x J_1^2 + \Lambda_1)/G_s, \quad T_{21}^\text{sv} = T_{21}, \quad T_{23}^\text{sv} = T_{23}.
\]

\( T_{23}^\text{sv} \) is the limitation of \( T_{12} \) for a classical large input \( \alpha_{\text{in}} \) and also valid for single-photon pulses. Thus, we can achieve ONR in both the classical and quantum regimes. Below, we assume \( \Delta_a = \Delta_0 = \Delta \) and \( \kappa_a = \kappa_b = \kappa \).

Next, we will show two different mechanisms to achieve a strong ONR dependence on the bare mode coupling rate \( J_0 \). When \( J_0 < \kappa \), the two resonators originally have no NMS. We use the pump field to induce the NMS between \( a_{\text{opt}} \) and \( b_{\text{opt}} \), namely, the NMS scenario. For \( J_0 > \kappa \) resulting in the NMS between the bare modes, we use the pump field to significantly shift the resonance frequency of the mode \( b_{\text{opt}} \). We call this mechanism the mode resonance shift (MRS) scenario. Under the optimal condition \([J_0^2 + \kappa^2] + (2\kappa_0 \Delta_0^2) \approx 0 \), we obtain near-zero \( T_{21} \) and thus the maximal isolation ratio

\[
\begin{align*}
\eta_{\text{max}} &\approx 10 \log_{10} \left[ \frac{1 - 2\kappa N_{\text{noise}}}{|\alpha_{\text{in}}|^2} \frac{4 J_0^4}{\kappa^2} \right] \\
\eta_{\text{max}} &\approx 10 \log_{10} \left[ \frac{1 + 2\kappa N_{\text{noise}}}{|\alpha_{\text{in}}|^2} \frac{J_0^2 \kappa^2}{(J_0^2 - \kappa^2) \kappa^2} \right],
\end{align*}
\]

at \( \Delta = 0 \) in the NMS scenario, where \( \sigma \approx 4 J_0^2 \kappa^2/[J_0^2 + \kappa^2 + 2 \kappa_0 \Delta_0^2] \) and \( \sigma \approx \kappa_{\text{ex}} \), or

\( \Delta \approx \sqrt{J_0^2 - \kappa^2} \) in the MRS scenario [53].

Our system can realize an optical diode with transmission \( T_{12} \gg T_{21} \) even with only the classical coherent pump \( \Omega_p \). For a weak input signal, e.g., \( \alpha_{\text{in}}/\sqrt{\kappa} = 0.6 \), the transmission \( T_{12} \) can be larger than unity, because of the pump-induced noise. When \( \alpha_{\text{in}}/\sqrt{\kappa} = 3 \), corresponding to an input including more than 9 photons within the resonator decay time, the input signal overwhelms the pump-induced noise. In this case, the transmission \( T_{12} \) in the classical regime approximates the noise-free transmission \( T_{12}^{\text{sv}} \) in the quantum regime. Below, we focus on the noise-free case, which is a good approximation of the classical case with a large input signal. In the NMS scenario, we choose \( J_0 = 0.99 \kappa \) for the optimal condition, such that the transmission \( T_{21} \) vanishes at \( \Delta = 0 \). In the forward-input case, the squeezing interaction enhances the coupling strength \( J_1 \) to much larger than the system decay rates and leads to a large NMS; see Fig. 2(a). Therefore, we obtain \( T_{12} \approx 83.1 \% \) and \( T_{21} \approx 0 \) at \( \Delta = 0 \), corresponding to an isolation ratio \( \eta^\text{sv} = 10 \log_{10} (T_{12}^{\text{sv}}/T_{21}^{\text{sv}}) \approx 85.1 \text{ dB} \), insertion loss \( L_{\text{sv}} = -10 \log_{10} (T_{12}^{\text{sv}}) \approx 0.80 \text{ dB} \). In the MRS scenario, we take \( J_0 = 2.8 \kappa \); for example, the transmission spectrum
three outputs, allowing photon flow along the direction of the resonator modes to high Fock states such that the spectrum is shifted with respect to the backward-input transmission, see Fig. 2(d). As a result, we attain a slightly larger pump power $\beta_p=86\%$ at $\Delta=0$, corresponding to $\tilde{L} \approx 0.43$ dB. We also obtain a similar performance in the NMS scenario with $T_{23} \approx 98.0\%$ at $\Delta/k=2.62$, corresponding to $\tilde{L} \approx 0.20$ dB. In both scenarios, we have $\mathcal{F} \approx 1$.

Our system can work as a single-photon quasicirculator when the squeezing-vacuum field is applied to cancel the noise term. We evaluate its performance for a single-photon wave packet input to ports 1 and 2 simultaneously by solving a quantum cascaded system [61–63] (also Supplemental Material [53]). We consider a Gaussian-like single-photon pulse with duration $2\pi \times 6\omega^{-1}$. In comparison with the case without the squeezed-vacuum field, the performance of our quasicirculator only slightly decreases. The fidelity is still very high, $\mathcal{F} \geq 98.7\%$. The insertion loss remains unchanged due to the large bandwidth in the NMS scenario. In comparison, it reduces to $\tilde{L} \approx 0.26$ dB at $\Delta/k=2.62$ in the MRS scenario. Therefore, our diode and quasicirculator can work in both the classical and quantum regimes.

When the pump laser with power $P_p$ is present, corresponding to ‘on’ (absent, corresponding to ‘off’), our device can switch on and off the transmission of a stronger signal laser from $T_{12}^m$ to $T_{12}^{off}$ according to Eq. (3), implying an all-optical nonreciprocal transistor. As the crucial role of electronic transistor in electric computers, optical transistors are essential for optical information processing [64–67]. We define the gain of the transistor as $G=P_{in}\Delta T/P_p$, with $\Delta T=T_{23}^m-T_{23}^{off}$ [64]. The gain increases linearly with the signal power. When we fix the pump strength, e.g., $\Omega_p/k=10$, in the NMS scenario, the gain of the transistor can reach $G>1$ ($G>100$) when $|\alpha_{in}|^2/k > 6.1 \times 10^7$ ($|\alpha_{in}|^2/k > 6.1 \times 10^6$), see Fig. 3(a). In the MRS scenario, we can obtain the same gain $G>1$ ($G>100$) by taking $\Omega_p/k=13$ and applying a slightly larger pump power $|\alpha_{in}|^2/k > 9.2 \times 10^7$.

![FIG. 2.](image) (a) and (d) Steady-state transmission versus the detuning $\Delta$. Dashed curves and open circles are for the analytical and numerical transmissions $T_{12}$ (blue), $T_{21}$ (red), and $T_{23}$ (green), respectively. Solid curves are for the corresponding numerical transmission of $T_{12}^n$, (b) and (e) Isolation ratio and insertion loss versus $r_p$, (c) and (f) Isolation ratio $\eta$ versus $\alpha_{in}$ and $\Delta$ (3D surface). Red curves and open circles are for analytical and numerical results. Black curves are for the maximum isolation ratio $\eta_{max}$ given by Eqs. (5), (6). (a), (b), and (e) for the NMS scenario ($J_0/k=0.99$); (d), (e), and (f) for the MRS scenario ($J_0/k=2.8$). Other parameters are $\kappa_{ext1,2}/k=0.99$; in (a) and (c) $\Delta^2_p/k=10.3$, $\Omega_p/k=10$, yielding $r_p \approx 1.05$; in (d) and (f) $\Delta_p/k=15$, $\Omega_p/k=13$, yielding $r_p \approx 0.66$; in (b) $\Delta=0$ and $\Delta_p/k=10$ sinh($r_p$); in (e) $\Delta/k=2.62$ and $\Delta_p/k=50$ sinh($r_p$).}

![FIG. 3.](image) Gain of the transistor versus detuning $\Delta$ and $P_{in}$. (a) The NMS scenario with $J_0/k=0.99$, $\Delta_p^m/k=10.3$, $\Omega_p/k=10$.
(b) The MRS scenario with $J_0/k=2.8$, $\Delta_p^m/k=15$, $\Omega_p/k=13$. Other parameters are $\kappa_{ext1,2}/k=0.99$, $g/k=10^{-3}$. 083604-4
(|\alpha_0|^2/\kappa > 9.2 \times 10^6), see Fig. 3(b). Unlike the forward-input case, the transmission \( T_{21} \) in the backward-input case is independent of the pump power and always vanishingly small. Clearly, our optical transistor is nonreciprocal.

Lithium-niobate-based microring resonators provide an excellent platform for our proposal, thanks to their large intrinsic loss rate \( \kappa \) and high optical quality factors up to \( Q \sim 10^7 \) [71,72]. Assuming an experimentally available intrinsic quality factor \( Q_i = 8 \times 10^6 \), the resonance frequency of the signal field \( \omega_0/2\pi = 193.4 \text{ THz} \) and the pump field frequency \( \omega_p \approx 2\omega_0 \) for the resonators, we obtain the intrinsic loss rate \( \kappa_i/2\pi = 24.2 \text{ MHz} \). By choosing an experimentally available gap \( \kappa \geq 20 \text{ dB} \) can reach 0.86\( \kappa_i/2\pi \approx 2.08 \text{ GHz} \) around \( \Delta = 0 \) (or \( 0.21\kappa_i/2\pi \approx 0.51 \text{ GHz} \) around \( \Delta = 2.62\kappa \)). The power of a pump field is given by \( P_p = h\omega_p^2\kappa_0^2\kappa_i^2/(16\pi^2\sigma_{ex}^2) \) [53], where \( \kappa_p \) and \( \kappa_{ex}^2 \) are, respectively, the total and external decay rates of the mode \( c_{ex} \), and \( g \) is the nonlinear single-photon coupling strength. The rate of \( g/2\pi = 2.35 \text{ MHz} \) is available for lithium-niobate-based microresonators [74]. The pump power \( P_p \approx 16.6 \text{ mW} \) (or 28.0 mW) yields to \( \Omega_p/\kappa = 10 \) (or 13). At the detuning \( \Delta/\kappa = 0 \) (or 2.62), we can induce an optical transistor with \( G > 1 \) for a signal power \( P_{in} \approx 18.9 \text{ mW} \) in the NMS scenario (or 28.5 mW in the MRS scenario). Because of inevitable imperfections in fabrication, it is not easy to precisely meet the optimal condition and the parameter relationships \( \Delta_a = \Delta_b^0 \) and \( \kappa_a = \kappa_b \). A small derivation of these conditions in fabrication may cause a slight reduction in the performance, particularly the isolation ratio of the nonreciprocal device.

We have proposed a squeezing-based scheme to realize a chip-compatible magnetic-free ONR, including an optical diode, a quasicirculator and a nonreciprocal optical transistor. The optical diode and circulator can work in the classical regime under a coherent pump and also in the quantum regime when a squeezed-vacuum field is applied. In particular, our work proposed the nonreciprocal optical transistor switching a strong signal with a weak control field. Such unconventional transistor cannot be realized in the configuration of Ref. [41] because a strong signal will cause NMs for the pump field. Our protocol paves a way for realizing on-chip all-optical nonreciprocal devices.

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