nature portfolio

Peer Review File



Open Access This file is licensed under a Creative Commons Attribution 4.0 International License, which permits use, sharing, adaptation, distribution and reproduction in any medium or format, as long as you give appropriate credit to

the original author(s) and the source, provide a link to the Creative Commons license, and indicate if changes were made. In the cases where the authors are anonymous, such as is the case for the reports of anonymous peer reviewers, author attribution should be to 'Anonymous Referee' followed by a clear attribution to the source work. The images or other third party material in this file are included in the article's Creative Commons license, unless indicated otherwise in a credit line to the material. If material is not included in the article's Creative Commons license and your intended use is not permitted by statutory regulation or exceeds the permitted use, you will need to obtain permission directly from the copyright holder. To view a copy of this license, visit <u>http://creativecommons.org/licenses/by/4.0/</u>.

REVIEWERS' COMMENTS

Reviewer #1 (Remarks to the Author):

4 5 Qualitative features of vector fields on the plane and in three-dimensional space are an important 6 part of the general theory of oscillations and waves. For example, in structured light, with 7 amplitude, phase, and polarization spatially varying, these can be woven into loops, links and 8 knots, and organize Möbius strips. Characterization of the topological properties of optical vector 9 electromagnetic fields is an extremely difficult task. The article proposes an original idea and a 10 new tool for the analysis of such fields, based on the construction of a three-dimensional skyrmion 11 hopfion in polarization and phase diagram of a propagating light beam. The experiments and 12 theory presented in the article demonstrate new topological invariants that are possible in a 13 structured light. Overall, the paper is well written, and I recommend it for publication.

14 15

1

2 3

16 Reviewer #2 (Remarks to the Author):

Mark Dennis and coworkers report on creating 3D Hopfions of Skyrmions in 3D structured light.

- 19 This manuscript is very topical and exciting and the results are extremely impressiv. The topic fits 20 in the scope of Nature Communications and should be published.
- 21 The results are extremely clean and convincing, the paper is very logically structured and clearly

22 written, and the additional information and the renderings (and movies) are beautiful.

23

24 The paper should be published in Nat Comm as is.